

# The astrophysics of extreme mass-ratio inspiral sources

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# Overview

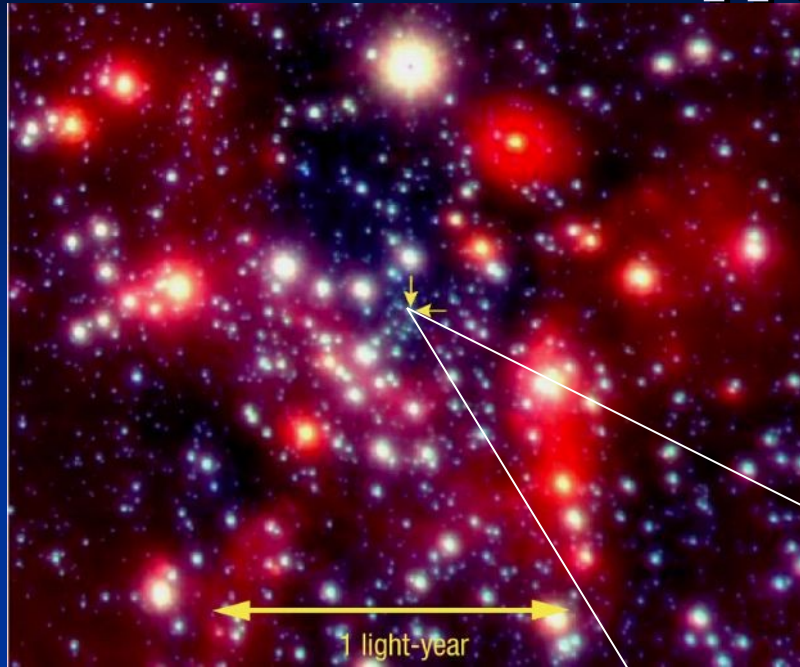
- Motivation: why EMRIs?
- Stellar dynamics and content near massive black holes
- Part I: the pure inspiral problem
  - Inspiral dynamics
  - A critical length scale
  - Mass segregation
  - Resonant relaxation
  - Eccentricity distribution
- Part II: alternative routes to EMRIs
  - EMRI formation in accretion disks
  - Binary disruption
  - Remnants of ultra-luminous X-ray sources

# Why are EMRIs important?

- Detailed tests for general relativity
- Stellar content very close to massive black holes
- Stellar dynamics very near massive black holes
- Mass distribution of massive black holes
- Spin distribution of massive black holes; merger history
- Accretion disks
- Do intermediate mass black holes exist?
- Are massive black holes really black holes?

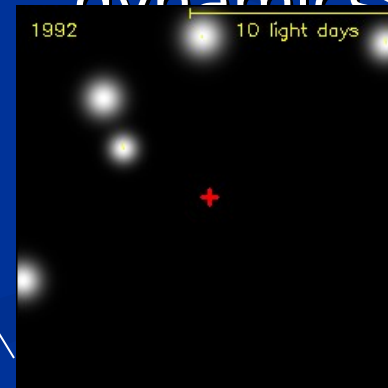
(Or, let's say, boson stars?)

# Stars near massive black holes



Infra-red observations of the Galactic center

- Very dense environment of stars
- Density diverges as a power-law:  $n \sim r^{-(1.5-2)}$  (Alexander 1999)
- Short relaxation times ( $t_r < 10$  Gyr)
- Black hole dominates dynamics within  $\sim 1$  pc.



See talks by  
**Tal Alexander**  
and **Melvyn Davis**

Bahcall & Wolf 1976, 1977;  
Alexander 1999; Genzel et al. 2003

# Part I

## The pure inspiral problem

**“What is the rate at which detectable  
forms in a system of single point particles  
near a massive black hole?”**

Hils & Bender 1995; Sigurdsson & Rees 1997; Miralda-Escude & Gould 2000  
Freitag 2001, 2003; Ivanov 2002; Gair et al 2004; Hopman & Alexander 2004  
De Freitas Pacheco et al. 2006

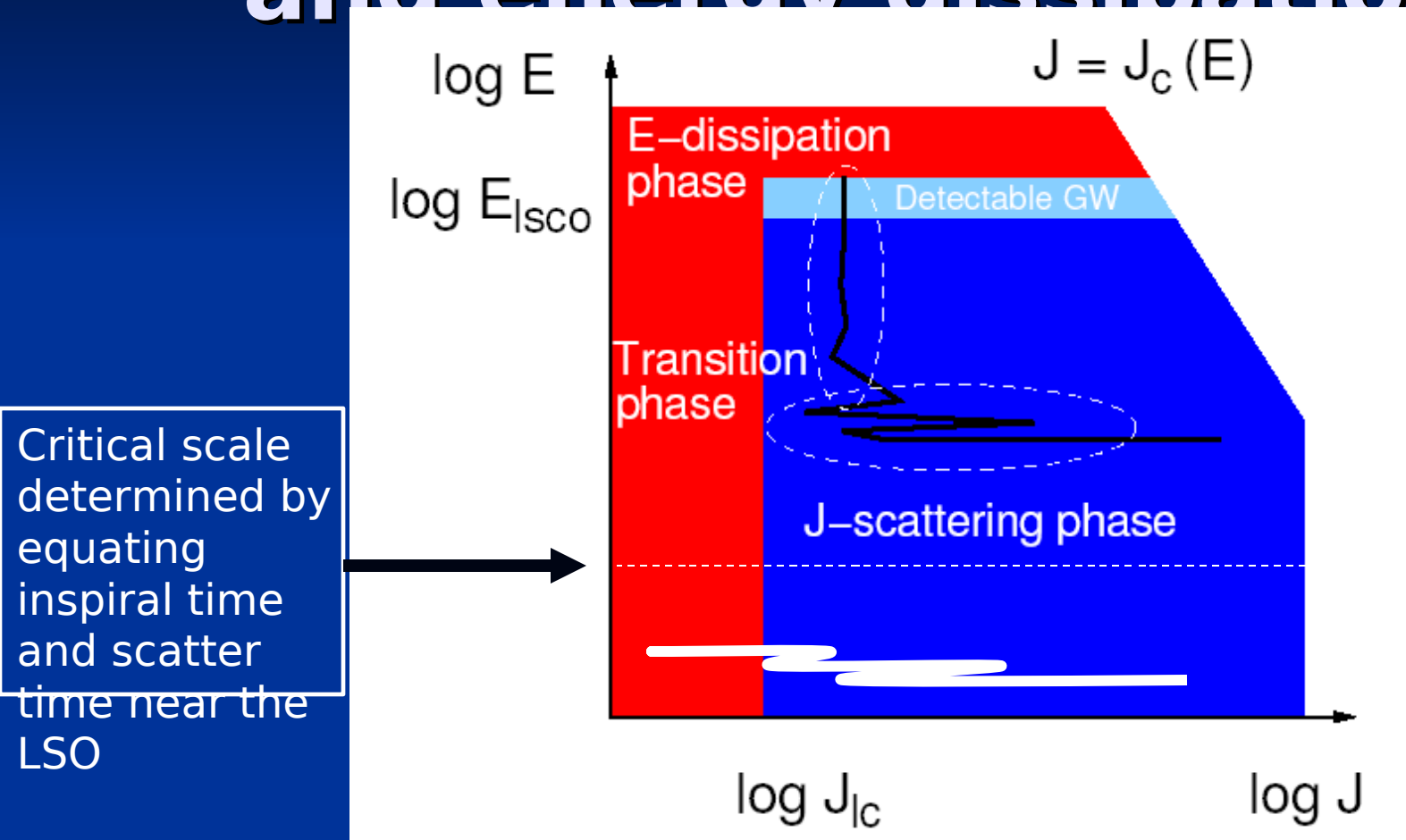
# How to get near a massive BH



Bursts of GWs  
may be  
observable in  
our own

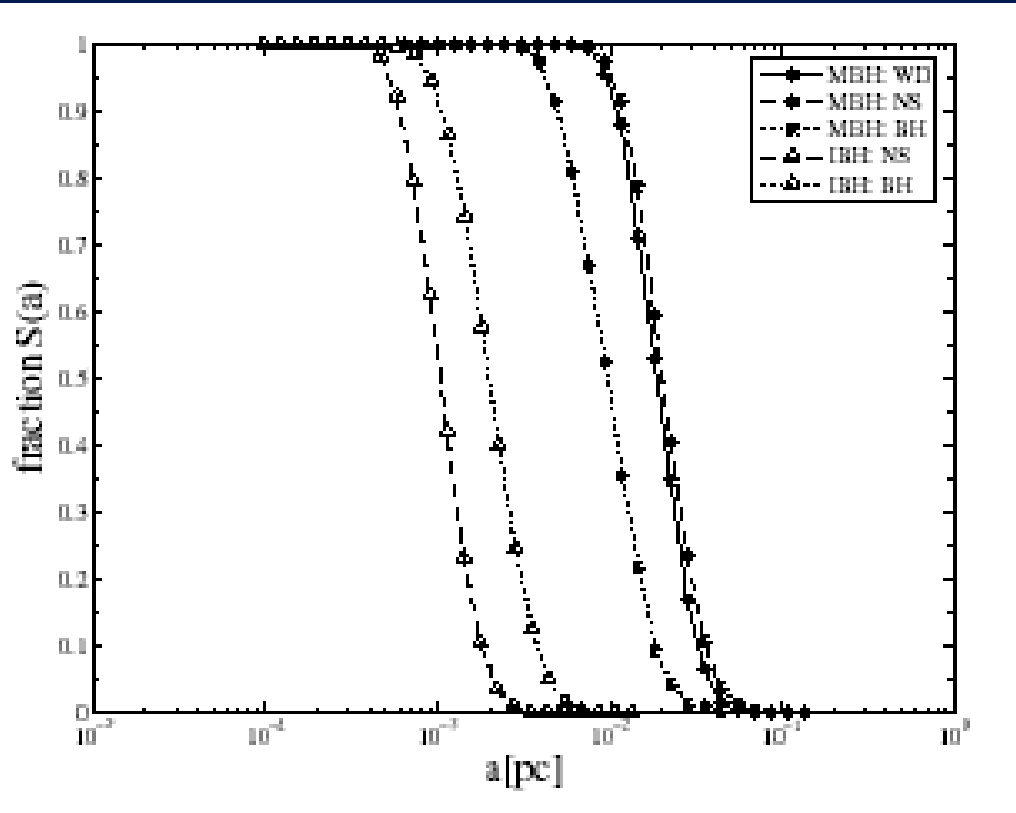
Galactic center  
(Rubbo et al.  
2006)

# Angular momentum scattering and energy dissipation



Hils & Bender (1995); Hopman & Alexander (2005)

# EMRI event rate

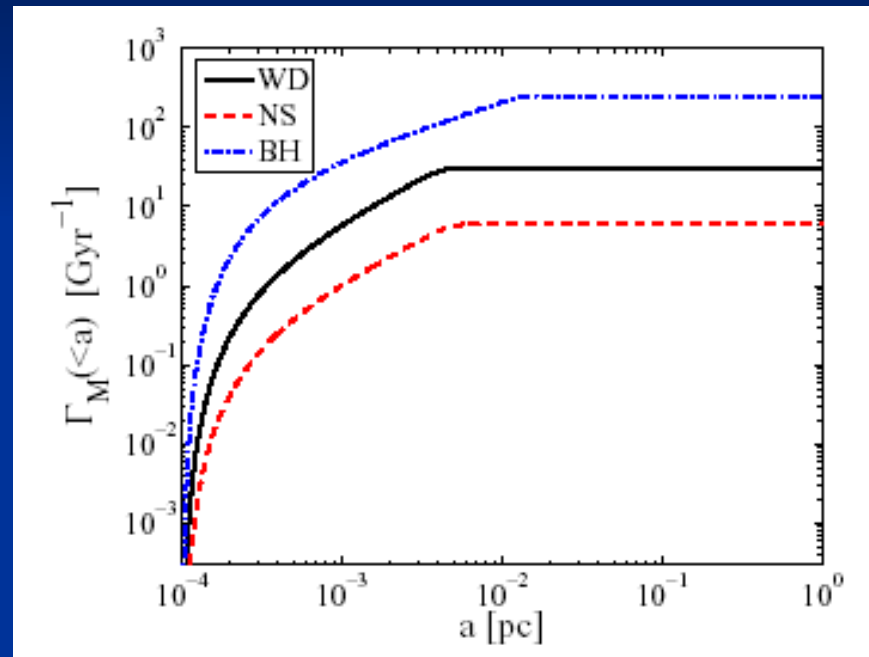
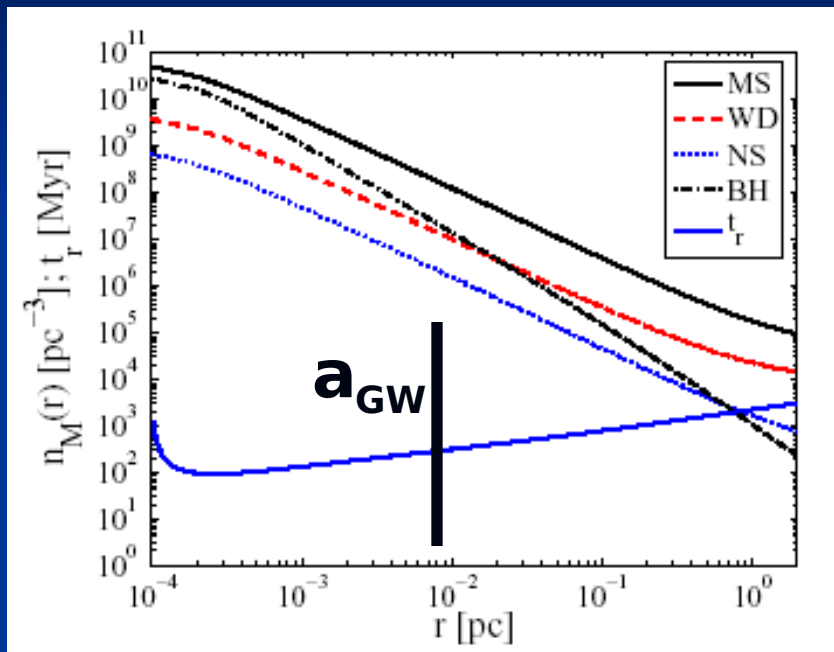


Hopman & Alexander (2005)

- Critical distance at  $a_{\text{GW}} = 0.01 \text{ pc}$
- Nature of EMRIs determined by dynamics  $< a_{\text{GW}}$
- Event rate: integrate diffusion expression over inspiral probability

$$\Gamma_i = f_s \int_0^\infty \frac{da N(a) S(a)}{\ln(J_m / J_{lc}) t_r(a)}$$

# Dynamics within $a_{\text{GW}}$ : mass segregation

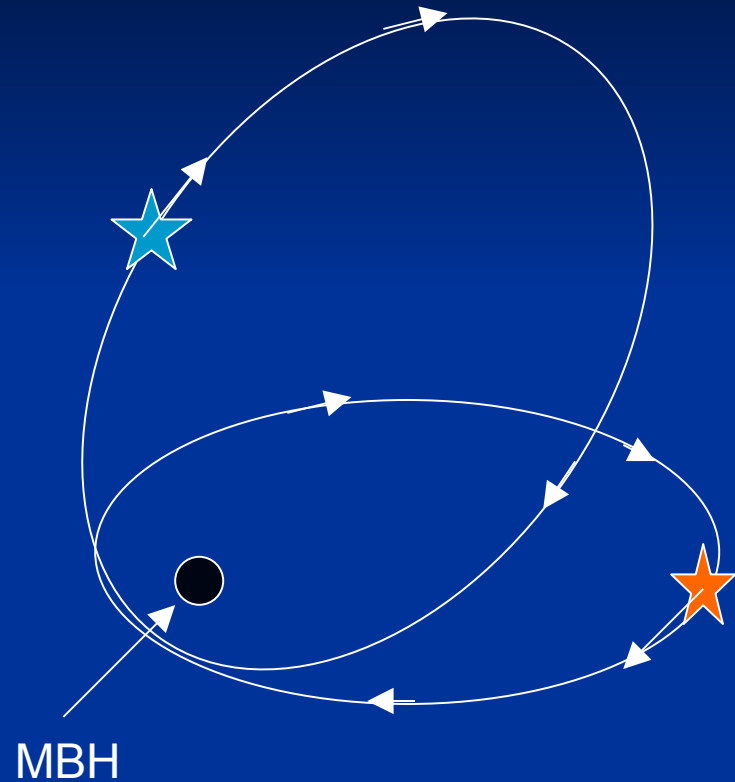


Stellar BHs sink to center and dominate dynamics within  
Relaxation time decreases due to presence of stellar BH

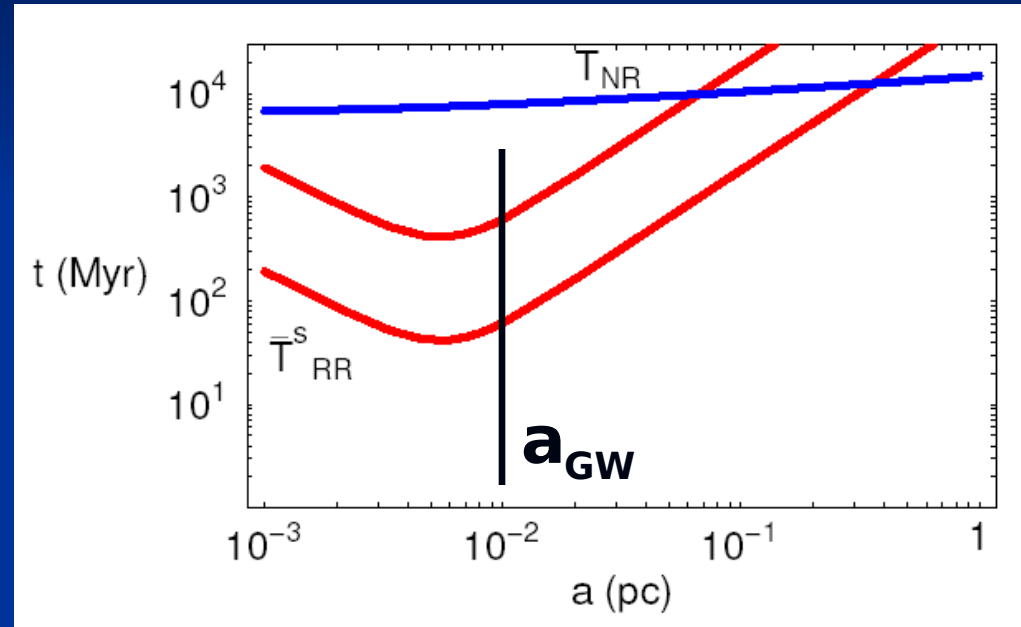
Hopman & Alexander (2006), Freitag, Amaro-Seoane & Kalogera (2006)

Clovis Hopman, Leiden observatory. Potsdam, September 2006

# Dynamics within $a_{\text{GW}}$ : resonant relaxation



$$T \sim (M_{\text{bh}}/M_{\text{s}})P(a)$$



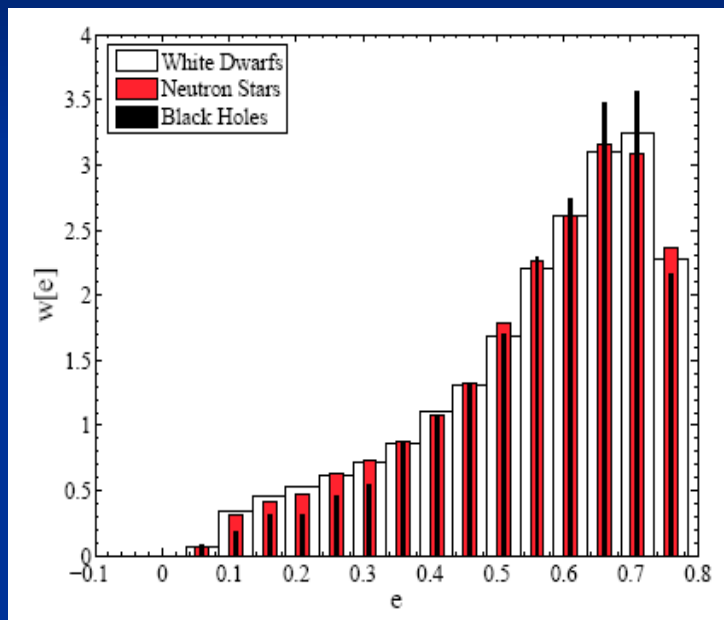
**Resonant relaxation increases EMRI by  
Crucial to include general relativity!**

Rauch & Tremaine (1995); Rauch & Ingalls (1998)

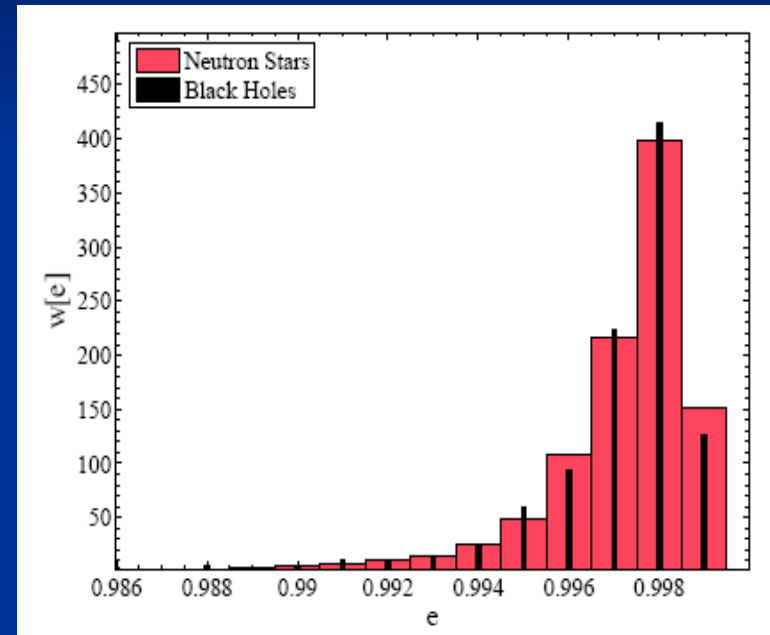
Hopman & Alexander (2006)

# LISA EMRIs: high eccentricities at P=3 hrs

Massive Black Holes:



Intermediate Mass Black Holes:



Hopman & Alexander (2005)

Orbits must be modeled (pseudo-)relativistically  
Hopman & Alexander 2005; Gair et al

# Issues that should be addressed

- Mass segregation (Freitag 2001, 2003, 2006; Hopman & Alexander 2006b)
- Resonant relaxation (Hopman & Alexander 2006a)
- Simultaneous energy and angular momentum (Freitag 2001, 2003, 2006)
- General relativistic inspiral (Hopman & Alexander; Gair et al 2005)
- High resolution of inspiral (Hopman & Alexander)
- Stellar dynamics beyond radius of influence (Freitag 2001, 2003, 2006)
- Stellar population dependence on host galaxy (De Freitas Pacheco et al. 2006).
- Deviations from spherical symmetry (nobody(?))
- Non-relaxed systems (nobody(?))

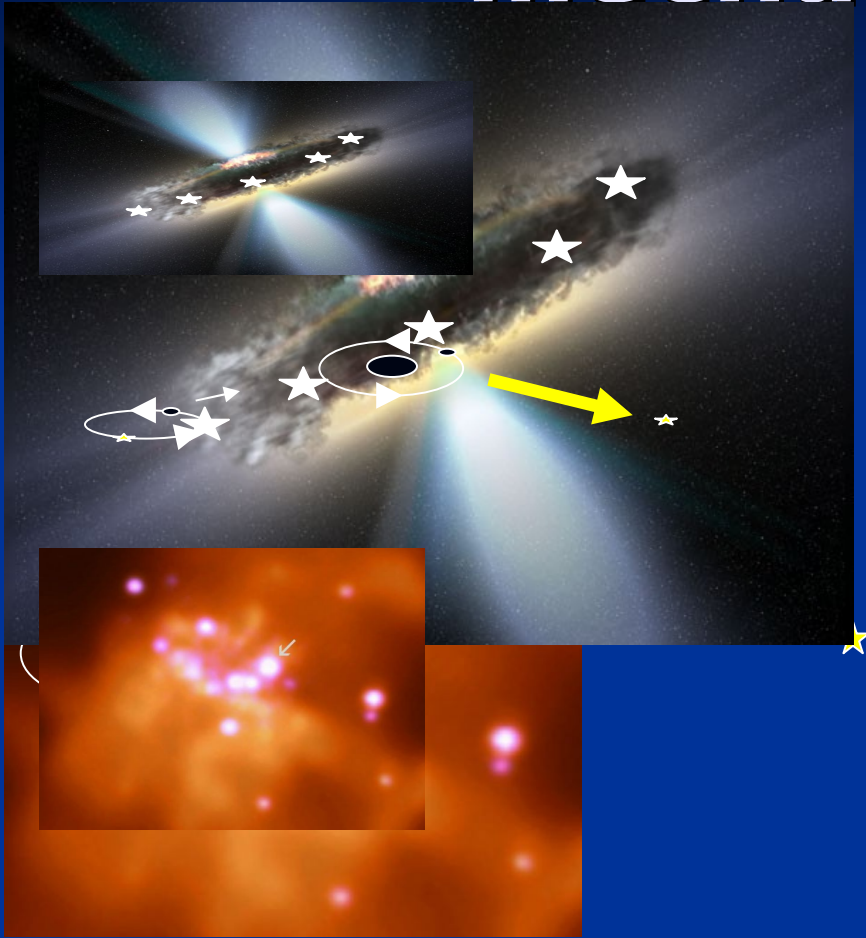
# Part II

## Alternative routes to EMRIs

**“What is the rate at which detectable  
form by other mechanisms than the p  
inspiral problem?”**

Levin 2003, 2006; Miller et al. 2005; Hopman & Portegies Zwart 20

# Indirect EMRI capture mechanisms



Stars can be formed in accretion disks and spiral in due to interaction with gas (Levin 2003, 2006)

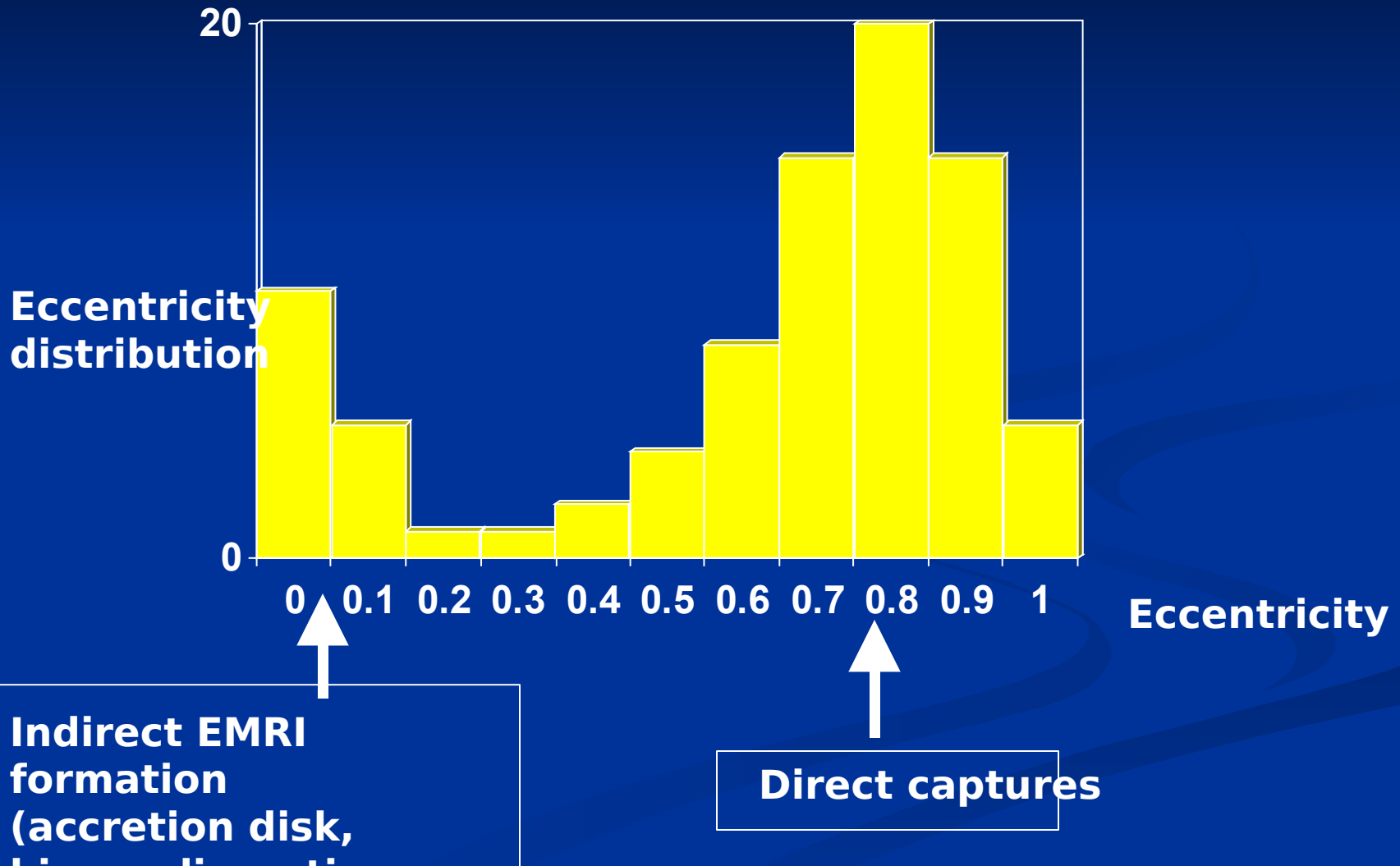
Binary stars are tidally disrupted, forming a hyper-velocity star and an EMRI (Miller, Freitag & Hamilton 2005)

Stars can be tidally captured by intermediate mass BHs. After an ultraluminous X-ray phase, they leave the main sequence and spiral in (Hopman et al 2004, Hopman & Portegies Zwart 2005)

Efficient loss cone refilling by triaxiality (Holley-Bockelman et al, 2006) and massive perturbers (Perets, Hopman & Alexander 2006)

**Indirect EMRI formation leads to *low* eccentricity**

# A bimodal distribution of eccentricities?



Indirect EMRI formation  
(accretion disk,  
binary disruption,  
tidal capture)

Direct captures

# Conclusions

- Direct captures: event rate of  $\sim 100/\text{Gyr}/\text{MBH}$ , but rather uncertain. Stellar BHs dominate rate
- Rates depend on dynamics within  $a_{\text{GW}} \sim 0.01$  pc: mass-segregation, resonant relaxation, ...
- Direct capture sources are eccentric
- Indirect capture leads to low eccentricity EMRIs